

# ELEC5470 - Convex Optimization

## Fall 2017-18, HKUST

### Basic Information

Instructor: Prof. Daniel P. Palomar (<http://www.danielpalomar.com>)

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ELEC5470 – Convex Optimization [3-0-0:3]

Website: <https://www.danielpalomar.com/elec5470---convex-optimization.html>

Lecture Time: Mon 18:00 - 20:50

Lecture Venue: Rm5583 (Lifts 27-30)

### Description

In the last three decades, a number of fundamental and practical results have been obtained in the area of convex optimization theory. It is a well-developed area, both in the theoretical and practical aspects, and the engineering community has greatly benefited from these recent advances by finding applications.

This graduate course introduces the basic theory and illustrates its use with many recent applications in signal processing, communication systems, machine learning, networking, robust design, image processing, financial engineering, etc. The emphasis will be on i) the art of unveiling the hidden convexity of problems by appropriate manipulations, and ii) a proper characterization of the solution either analytically or algorithmically. The course follows a case-study approach by considering recent successful applications of convex optimization published within the last decade in top scientific journals.

Problems will be covered in areas of signal processing such as filter/beamforming design, circuit design, robust designs under uncertainty, sparsity optimization, low-rank optimization, image processing, classification methods, portfolio optimization in financial systems, discrete maximum likelihood decoding, transceiver design for MIMO channels, cognitive radio systems, network optimization, distributed algorithms, wireless network power control, Internet protocol design, etc.

### Textbooks

- S. Boyd and L. Vandenberghe, *Convex Optimization*, Cambridge University Press, 2004.  
[<http://www.stanford.edu/~boyd/cvxbook/>]
- Daniel P. Palomar and Yonina C. Eldar, *Convex Optimization in Signal Processing and Communications*, Cambridge University Press, 2009.
- D. P. Bertsekas, *Nonlinear Programming*, Athena Scientific, Belmont, Massachusetts, 2<sup>nd</sup> Ed., 1999.

### Prerequisite:

Students are expected to have a solid background in linear algebra and know basic signal processing. They are also expected to have research experience in their particular area and be capable of reading and dissecting scientific papers.

### Grading:

Homework: 10%

Quizzes: 10% (auditors too)

Midterm: 20% (auditors too)

Final Project: 60% (homeworks and midterm are required to be passed)

## Course Schedule

Date	Week	Lec	Topic	HM
3-Sep	1	1	Introduction	
		2	Theory: convex sets and convex functions	
10-Sep	2	3	Theory: convex problems and classes of convex problems (LP, QP, SOCP, SDP, GP)	
		4	Application: norm minimiz. with applications to image processing	HM1
21-Sep	3	5	Application: filter design	
		6	Theory: disciplined convex programming - cvx	HM2
24-Sep	4	7	Theory: Lagrange duality and KKT conditions	
		8	Application: waterfilling solutions	HM3
8-Oct	5	9	Theory: numerical algorithms – interior point method	
		10	Application: worst-case robust beamforming	HM4
15-Oct	6	11	Theory: MM-based algorithms	
		12	Theory&Application: Geometric Programming (GP)	
22-Oct	7	13	Application: sparsity via $l_1$ -norm minimization	
		14	Application: sparse index tracking in finance	
29-Oct	8		Midterm	
5-Nov	9	15	Application: classification and SVM in machine learning	
		16	Application: ML decoding via SDP relaxation	
12-Nov	10	17	Application: rank-constrained SDP and multiuser downlink beamforming	
		18	Application: low-rank optimization problems (Netflix, video security)	
19-Nov	11	19	Theory: primal/dual decompositions techniques	
		20	Application: alternative decompositions for NUM in wired and wireless networks	
26-Nov	12	21	Application: the Internet as a convex optimization problem	
		22	Application: blind separation via convex optimization in image proc.	

	extra	Application: portfolio optimization in financial engineering
		Application: MIMO transceivers based on Majorization Theory
		Theory: numerical algorithms – cutting plane and ellipsoid methods
		Application: segmentation and Multiview Reconstruction in Image Processing
		Application: multiuser MIMO transceiver design
		Application: dual decomposition for sum-power sum-capacity of MIMO MAC (IWFA)
		Application: primal decomposition for multicarrier MIMO transceiver design
		Theory: the S-procedure for robust design
		Theory: minimax problems
		Theory: nonconvex optimization and complexity (NP-ities)
		Theory: Variational Inequality Theory
		Application: Cognitive Radio Systems via Variational Inequality